

Please check the examination details below before entering your candidate information

Candidate surname

Other names

Centre Number

Candidate Number

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## Pearson Edexcel International Advanced Level

Time 1 hour 30 minutes

Paper

reference

**WFM01/01**

### Mathematics

**International Advanced Subsidiary/Advanced Level  
Further Pure Mathematics F1**

**You must have:**

Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

#### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided – *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

#### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 9 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets – *use this as a guide as to how much time to spend on each question.*

#### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

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Q:1/1/1/



  
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**Question 1 continued**

Lined writing area for the answer to Question 1.

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**(Total for Question 1 is 6 marks)**



2.

$$f(x) = 10 - 2x - \frac{1}{2\sqrt{x}} - \frac{1}{x^3} \quad x > 0$$

- (a) Show that the equation  $f(x) = 0$  has a root  $\alpha$  in the interval  $[0.4, 0.5]$  (2)
- (b) Determine  $f'(x)$ . (3)
- (c) Using  $x_0 = 0.5$  as a first approximation to  $\alpha$ , apply the Newton-Raphson procedure once to  $f(x)$  to find a second approximation to  $\alpha$ , giving your answer to 3 decimal places. (2)

The equation  $f(x) = 0$  has another root  $\beta$  in the interval  $[4.8, 4.9]$

- (d) Use linear interpolation once on the interval  $[4.8, 4.9]$  to find an approximation to  $\beta$ , giving your answer to 3 decimal places. (2)

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**Question 2 continued**

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3.  $\mathbf{M} = \begin{pmatrix} k & k \\ 3 & 5 \end{pmatrix}$  where  $k$  is a non-zero constant

(a) Determine  $\mathbf{M}^{-1}$ , giving your answer in simplest form in terms of  $k$ . (2)

Hence, given that  $\mathbf{N}^{-1} = \begin{pmatrix} k & k \\ 4 & -1 \end{pmatrix}$

(b) determine  $(\mathbf{MN})^{-1}$ , giving your answer in simplest form in terms of  $k$ . (2)

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Question 3 continued

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(Total for Question 3 is 4 marks)





**Question 4 continued**

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**Question 4 continued**

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**(Total for Question 4 is 8 marks)**









**Question 5 continued**

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6. The parabola  $C$  has equation  $y^2 = 36x$

The point  $P(9t^2, 18t)$ , where  $t \neq 0$ , lies on  $C$

(a) Use calculus to show that the normal to  $C$  at  $P$  has equation

$$y + tx = 9t^3 + 18t \tag{4}$$

(b) Hence find the equations of the two normals to  $C$  which pass through the point  $(54, 0)$ , giving your answers in the form  $y = px + q$  where  $p$  and  $q$  are constants to be determined. (4)

Given that

- the normals found in part (b) intersect the directrix of  $C$  at the points  $A$  and  $B$
- the point  $F$  is the focus of  $C$

(c) determine the area of triangle  $AFB$  (3)

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**Question 6 continued**

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7.

$$\mathbf{A} = \begin{pmatrix} -\frac{\sqrt{3}}{2} & -\frac{1}{2} \\ \frac{1}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix}$$

(a) Determine the matrix  $\mathbf{A}^2$  (1)

(b) Describe fully the single geometrical transformation represented by the matrix  $\mathbf{A}^2$  (2)

(c) Hence determine the smallest positive integer value of  $n$  for which  $\mathbf{A}^n = \mathbf{I}$  (1)

The matrix  $\mathbf{B}$  represents a stretch scale factor 4 parallel to the  $x$ -axis.

(d) Write down the matrix  $\mathbf{B}$  (1)

The transformation represented by matrix  $\mathbf{A}$  followed by the transformation represented by matrix  $\mathbf{B}$  is represented by the matrix  $\mathbf{C}$

(e) Determine the matrix  $\mathbf{C}$  (2)

The parallelogram  $P$  is transformed onto the parallelogram  $P'$  by the matrix  $\mathbf{C}$

(f) Given that the area of parallelogram  $P'$  is 20 square units, determine the area of parallelogram  $P$  (2)

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Question 7 continued

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Question 7 continued

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8. (a) Use the standard results for  $\sum_{r=1}^n r^2$  and  $\sum_{r=1}^n r$  to show that for all positive integers  $n$

$$\sum_{r=0}^n (r+1)(r+2) = \frac{1}{3}(n+1)(n+2)(n+3) \quad (5)$$

- (b) Hence determine the value of

$$10 \times 11 + 11 \times 12 + 12 \times 13 + \dots + 100 \times 101 \quad (3)$$









9. (i) A sequence of numbers is defined by

$$u_1 = 3$$

$$u_{n+1} = 2u_n - 2^{n+1} \quad n \geq 1$$

Prove by induction that, for  $n \in \mathbb{N}$

$$u_n = 5 \times 2^{n-1} - n \times 2^n \tag{5}$$

(ii) Prove by induction that, for  $n \in \mathbb{N}$

$$f(n) = 5^{n+2} - 4n - 9$$

is divisible by 16

(5)







**Question 9 continued**

Lined area for writing the answer to Question 9.

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**Question 9 continued**

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**(Total for Question 9 is 10 marks)**

**TOTAL FOR PAPER: 75 MARKS**

**END**

